

# SU(3)-FLAVOR TMD PDFS EXTRACTION WITH GLOBAL FITS & ANN

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U.S. DEPARTMENT OF  
**ENERGY**

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# OUTLINE

- A brief Introduction to TMD PDFs
- Sivers Function
- Sivers asymmetry from SIDIS
- Sivers asymmetry from DY
- Global analyses of Sivers function
- Fitting methodology
- Neural Network approach with SIDIS
- Fit results to SIDIS
- Fit results to SIDIS & DY
- Discussion & Future work

# TMD PDFs

		Quark Polarization		
		U	L	T
Nucleon Polarization	U	$f_1 = \odot$	N/A	$h_1^\perp = \odot - \ominus$ Boer-Mulders
	L	N/A	$g_{1L} = \odot - \ominus$ Helicity	$h_{1L}^\perp = \odot - \ominus$
	T	$f_{1T}^\perp = \odot - \ominus$ Sivers	$g_{1T}^\perp = \odot - \ominus$	$h_1 = \odot - \ominus$ $h_{1T}^\perp = \odot - \ominus$ Transversity

$$\Phi(x, k_T; S) = \int \frac{d\xi^- d\xi_T}{(2\pi)^3} e^{ik \cdot \xi} \langle P, S | \bar{\psi}(0) \mathcal{U}_{[0, \xi]} \psi(\xi) | P, S \rangle |_{\xi^+ = 0}$$

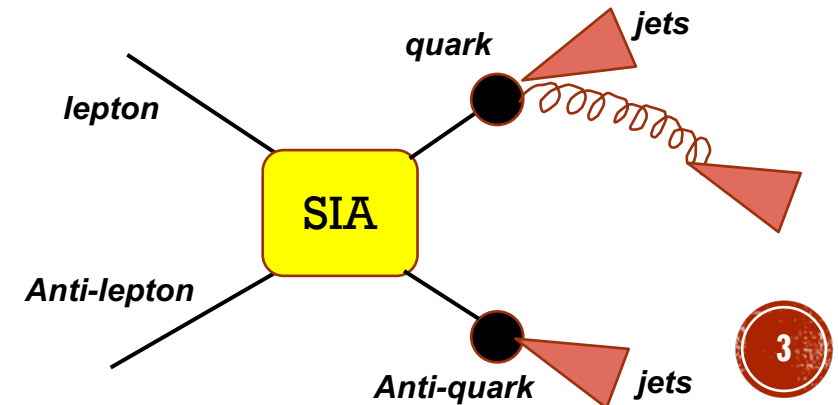
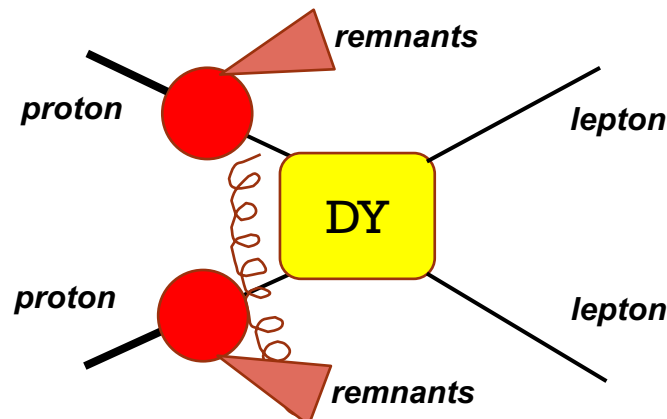
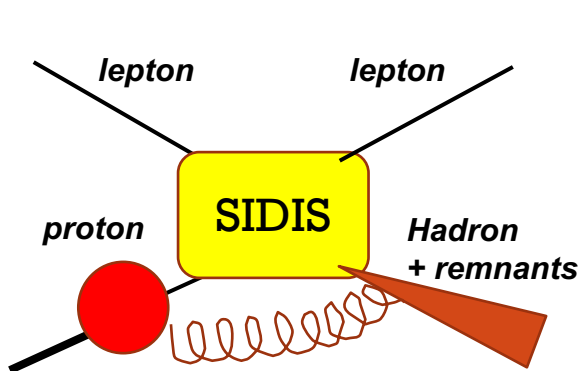
Quark correlator can be decomposed into 8 components  
(6 T-even and 2 T-odd terms) at leading-twist

$$\begin{aligned} \Phi(x, k_T, P, S) = & f_1(x, k_T^2) \frac{\not{P}}{2} + \frac{h_{1T}(x, k_T^2)}{4} \gamma_5 [\not{S}_T, \not{P}] + \frac{S_L}{2} g_{1L}(x, k_T^2) \gamma_5 \not{P} + \frac{k_T \cdot S_T}{2M} g_{1T}(x, k_T^2) \gamma_5 \not{P} \\ & + S_L h_{1L}^\perp(x, k_T^2) \gamma_5 \frac{[k_T, \not{P}]}{4M} + \frac{k_T \cdot S_T}{2M} h_{1T}^\perp(x, k_T^2) \gamma_5 \frac{[k_T, \not{P}]}{4M} \end{aligned}$$

T-even

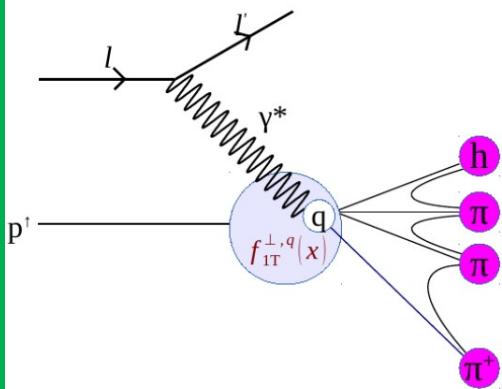
$$+ i h_1^\perp(x, k_T^2) \frac{[k_T, \not{P}]}{4M} - \frac{\epsilon_T^{k_T S_T}}{4M} f_{1T}^\perp(x, k_T^2) \not{P}$$

T-odd



# TMD PDFS

## Polarized Semi-Inclusive DIS



## SIDIS

$$\frac{d\sigma_{SIDIS}^{LO}}{dx dy dz dp_T^2 d\varphi_h d\psi} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] \times (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \cos 2\phi_h (\varepsilon A_{UU}^{\cos 2\phi_h}) \right. \\ \left. + S_T \begin{bmatrix} \sin(\phi_h - \phi_S) (A_{UT}^{\sin(\phi_h - \phi_S)}) \\ + \sin(\phi_h + \phi_S) (\varepsilon A_{UT}^{\sin(\phi_h + \phi_S)}) \\ + \sin(3\phi_h - \phi_S) (\varepsilon A_{UT}^{\sin(3\phi_h - \phi_S)}) \end{bmatrix} \right\}$$

PDF  $\otimes$  FF

$$A_{UU}^{\cos 2\phi_h} \propto h_1^{\perp q} \otimes H_{1q}^{\perp h}$$

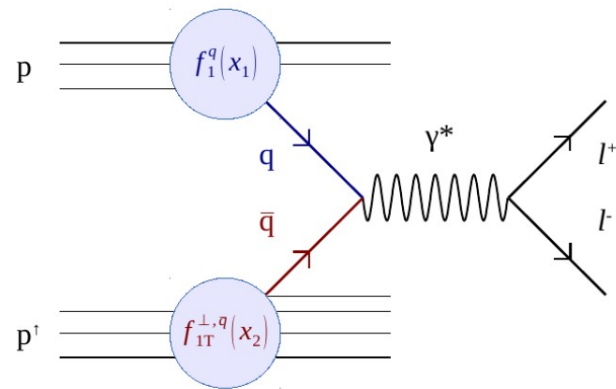
$$A_{UT}^{\sin(\phi_h - \phi_S)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$$

$$A_{UT}^{\sin(\phi_h + \phi_S)} \propto h_1^q \otimes H_{1q}^{\perp h}$$

$$A_{UT}^{\sin(3\phi_h - \phi_S)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

BM  $\otimes$  CF  
Sivers  $\otimes$  FF  
Transv  $\otimes$  CF  
Pretz  $\otimes$  CF

## Polarized Drell-Yan



## DY

$$\frac{d\sigma^{LO}}{d\Omega} = \frac{\alpha_{em}^2}{Fq^2} F_U^1 \left\{ 1 + \cos^2 \theta + \sin^2 \theta \cos 2\varphi_{CS} A_U^{\cos 2\varphi_{CS}} \right. \\ \left. + S_T \begin{bmatrix} (1 + \cos^2 \theta) \sin \varphi_S A_T^{\sin \varphi_S} \\ + \sin^2 \theta \left( \begin{matrix} \sin(2\varphi_{CS} + \varphi_S) A_T^{\sin(2\varphi_{CS} + \varphi_S)} \\ + \sin(2\varphi_{CS} - \varphi_S) A_T^{\sin(2\varphi_{CS} - \varphi_S)} \end{matrix} \right) \end{bmatrix} \right\}$$

beam target

PDF  $\otimes$  PDF

BM  $\otimes$  BM  
 $f_1$   $\otimes$  Sivers  
BM  $\otimes$  Transv  
BM  $\otimes$  Pretz

$$A_T^{\cos 2\varphi_{CS}} \propto h_1^{\perp q} \otimes h_1^{\perp q}$$

$$A_T^{\sin \varphi_S} \propto f_1^q \otimes f_{1T}^{\perp q}$$

$$A_T^{\sin(2\varphi_{CS} - \varphi_S)} \propto h_1^{\perp q} \otimes h_{1T}^{\perp q}$$

$$A_T^{\sin(2\varphi_{CS} + \varphi_S)} \propto h_1^{\perp q} \otimes h_1^q$$

$$h_1^{\perp q} \Big|_{SIDIS} = -h_1^{\perp q} \Big|_{DY}$$

$$f_{1T}^{\perp q} \Big|_{SIDIS} = -f_{1T}^{\perp q} \Big|_{DY}$$

$$h_1^q \Big|_{SIDIS} = h_1^q \Big|_{DY}$$

$$h_{1T}^{\perp q} \Big|_{SIDIS} = h_{1T}^{\perp q} \Big|_{DY}$$

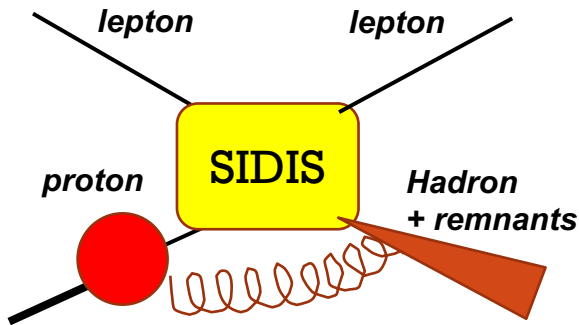
\* For these two processes TMD factorization is proven



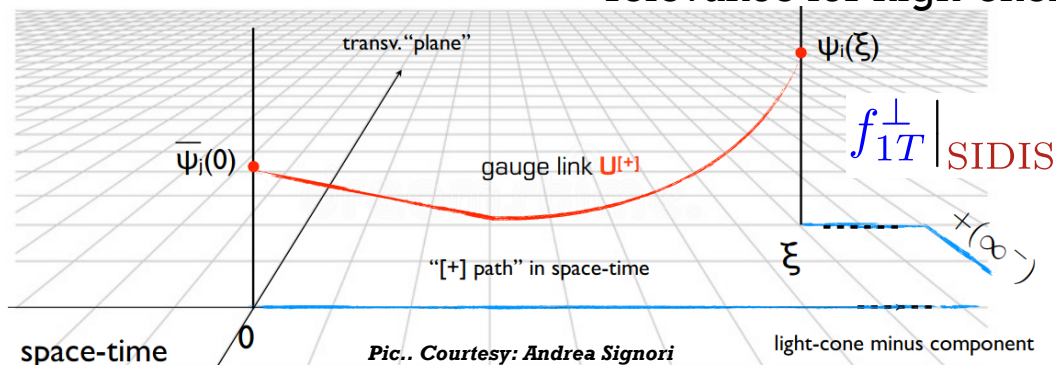
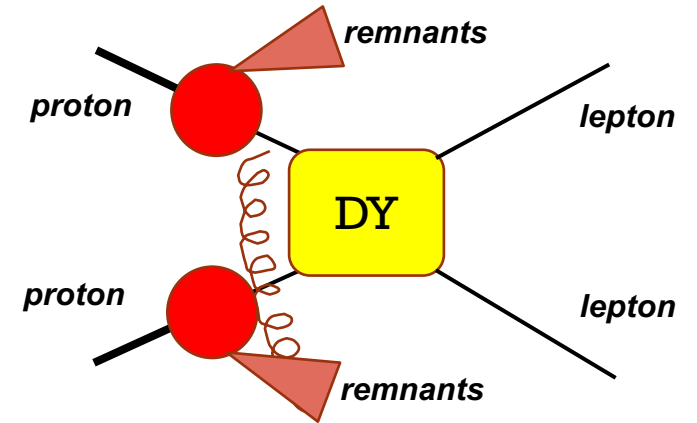
# SIVERS FUNCTION

$$f_{q/p^\uparrow}(x, \mathbf{k}_T) = f_{q/p}(x, \mathbf{k}_T) + f_{1T}^\perp(x, \mathbf{k}_T) \mathbf{S} \cdot (\hat{\mathbf{P}} \times \hat{\mathbf{k}}_T)$$

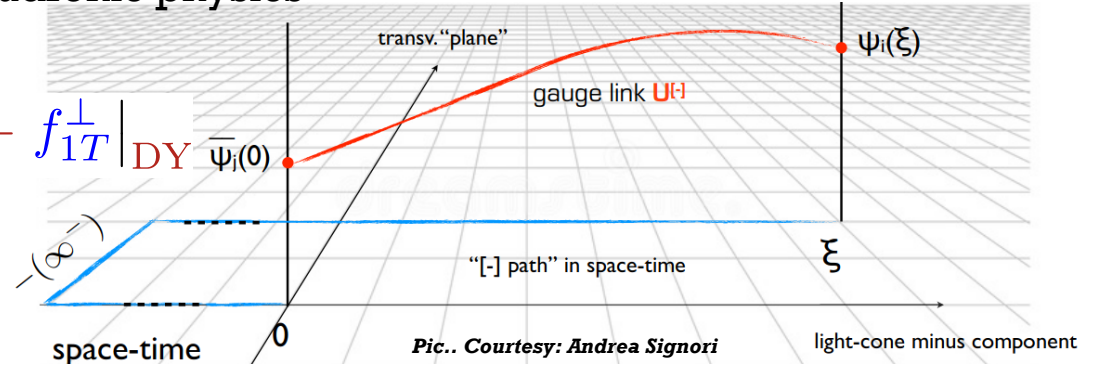
The Sivers function describes the correlation between the momentum direction of the struck quark and the spin of its parent nucleon.



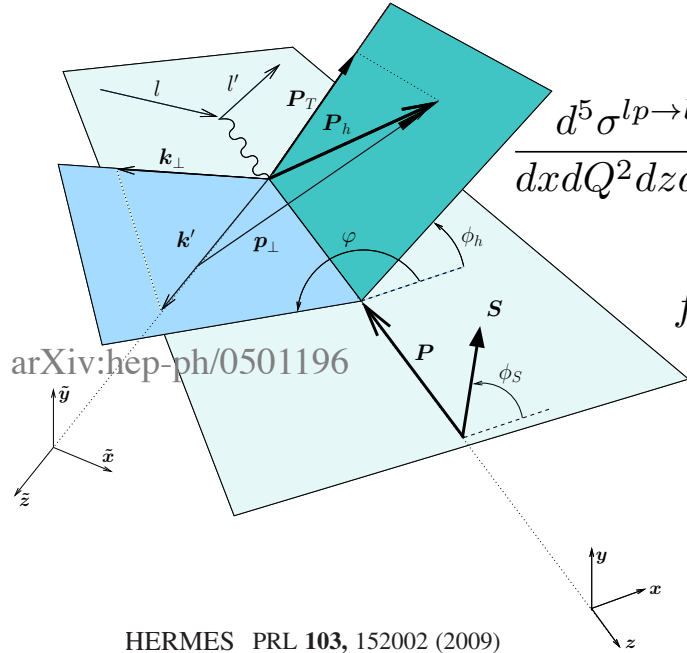
- The gauge-invariant definition of the Sivers function predicts the opposite sign for the Sivers function in SIDIS compared to processes with color charges in the initial state and a colorless final state in Drell-Yan,  $J/\psi, W^\pm, Z$
- This inclusion of the gauge link has profound consequences on factorization proofs and on the concept of universality, which are of fundamental relevance for high-energy hadronic physics



$$f_{1T}^\perp |_{\text{SIDIS}} = -$$

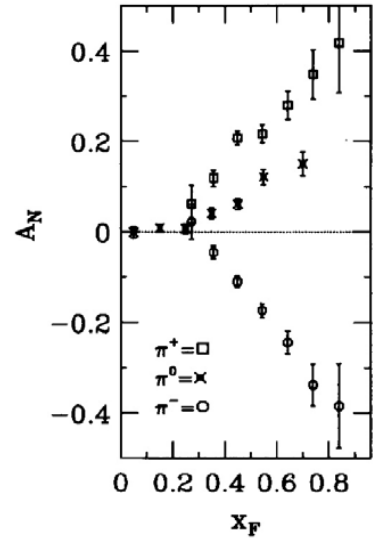


# SIVERS ASYMMETRY FROM SIDIS



$$\frac{d^5 \sigma^{lp \rightarrow lhX}}{dx dQ^2 dz d^2 p_{hT}} \propto \sum_q e_q^2 \int d^2 \mathbf{k}_\perp \mathcal{K}(x, p_{hT}, Q^2) f_q(x, \mathbf{k}_\perp) D_{h/q}(z, p_\perp) + \mathcal{O}(\mathbf{k}_\perp/Q)$$

$$\begin{aligned} f_{q/p\uparrow}(x, \mathbf{k}_\perp) &= f_{q/p}(x, k_\perp) + \frac{1}{2} \Delta^N f_{q/p\uparrow}(x, k_\perp) \mathbf{S} \cdot (\hat{\mathbf{p}} \times \hat{\mathbf{k}}_\perp) \\ &= f_{q/p}(x, k_\perp) - \frac{k_\perp}{m_p} f_{1T}^\perp(x, k_\perp) \mathbf{S} \cdot (\hat{\mathbf{p}} \times \hat{\mathbf{k}}_\perp) \end{aligned}$$



Asymmetry in  $pp^\uparrow \rightarrow \pi X$  pion production from E704

## Single Spin Asymmetry (Sivers Asymmetry)

$$A_{UT}^{\sin(\phi_h - \phi_s)}(x, y, z, p_{hT}) = \frac{d\sigma^{l\uparrow p \rightarrow hlX} - d\sigma^{l\downarrow p \rightarrow hlX}}{d\sigma^{l\uparrow p \rightarrow hlX} + d\sigma^{l\downarrow p \rightarrow hlX}} \equiv \frac{d\sigma_\uparrow - d\sigma_\downarrow}{d\sigma_\uparrow + d\sigma_\downarrow}$$

$$\begin{aligned} A_{UT}^{\sin(\phi_h - \phi_s)}(x, y, z, p_{hT}) &= \frac{[z^2 \langle k_\perp^2 \rangle + \langle p_\perp^2 \rangle] \langle k_S^2 \rangle^2}{[z^2 \langle k_S^2 \rangle + \langle p_\perp^2 \rangle] \langle k_\perp^2 \rangle^2} \exp \left[ -\frac{p_{hT}^2 z^2 (\langle k_S^2 \rangle - \langle k_\perp^2 \rangle)}{(z^2 \langle k_S^2 \rangle + \langle p_\perp^2 \rangle) (z^2 \langle k_\perp^2 \rangle + \langle p_\perp^2 \rangle)} \right] \\ &\times \frac{\sqrt{2e} z p_{hT} \sum_q \mathcal{N}_q e_q^2 f_q(x) D_{h/q}(z)}{M_1 \sum_q e_q^2 f_q(x) D_{h/q}(z)} \end{aligned}$$

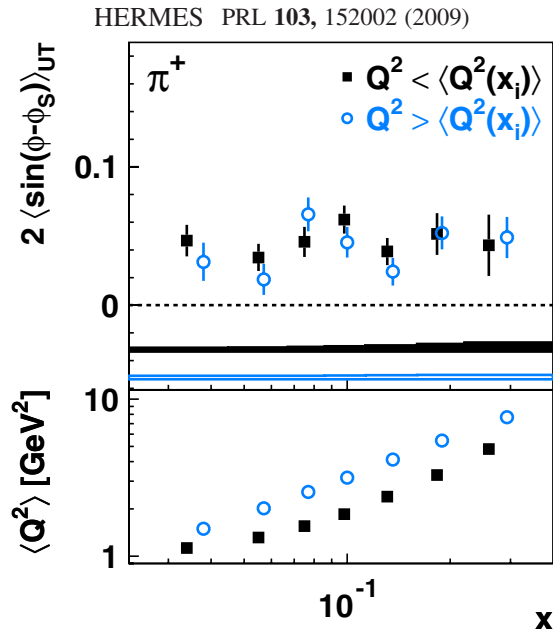
$$\langle p_\perp^2 \rangle = 0.12 \pm 0.01 \text{ GeV}^2$$

$$\langle k_\perp^2 \rangle = 0.57 \pm 0.08 \text{ GeV}^2$$

$$A_{UT}^{\sin(\phi_h - \phi_s)}(x, y, z, p_{hT}) = \mathcal{A}_0(z, p_{hT}, M_1) \left( \frac{\sum_q \mathcal{N}_q e_q^2 f_q(x) D_{h/q}(z)}{\sum_q e_q^2 f_q(x) D_{h/q}(z)} \right)$$

$$\mathcal{N}_q(x) = N_q x^{\alpha_q} (1-x)^{\beta_q} \frac{(\alpha_q + \beta_q)^{(\alpha_q + \beta_q)}}{\alpha_q^{\alpha_q} \beta_q^{\beta_q}}$$

$$\mathcal{N}_{\bar{q}}(x) = N_{\bar{q}}$$



# SIVERS ASYMMETRY FROM DRELL-YAN

$$f_{q/p}(x, k_{\perp}) = f_q(x) \frac{1}{\pi \langle k_{\perp}^2 \rangle} e^{-k_{\perp}^2 / \langle k_{\perp}^2 \rangle} \quad \langle k_{\perp}^2 \rangle = 0.25 \text{ GeV}^2$$

$$\begin{aligned} \Delta^N f_{q/p^{\uparrow}}(x, k_{\perp}) &= 2 \mathcal{N}_q(x) h(k_{\perp}) f_{q/p}(x, k_{\perp}) \\ &\equiv \Delta^N f_{q/p^{\uparrow}}(x) h(k_{\perp}) \frac{1}{\pi \langle k_{\perp}^2 \rangle} e^{-k_{\perp}^2 / \langle k_{\perp}^2 \rangle} \end{aligned}$$

$$\mathcal{N}_q(x) = N_q x^{\alpha_q} (1-x)^{\beta_q} \frac{(\alpha_q + \beta_q)^{(\alpha_q + \beta_q)}}{\alpha_q^{\alpha_q} \beta_q^{\beta_q}}$$

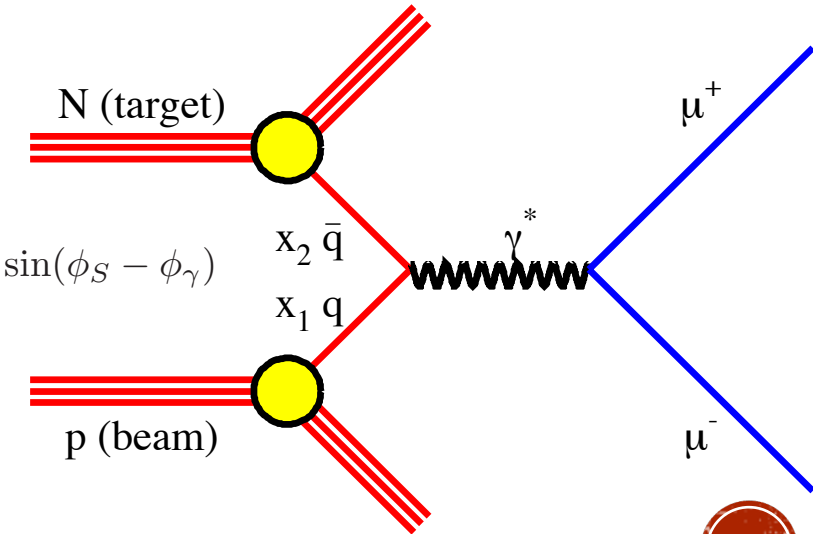
$$h(k_{\perp}) = \sqrt{2e} \frac{k_{\perp}}{M_1} e^{-k_{\perp}^2 / M_1^2}.$$

$$\frac{1}{\langle k_S^2 \rangle} = \frac{1}{M_1^2} + \frac{1}{\langle k_{\perp 1}^2 \rangle}$$

$$A_N^{\sin(\phi_{\gamma} - \phi_S)}(x_F, M, q_T) = \frac{\int d\phi_{\gamma} [N(x_F, M, q_T, \phi_{\gamma})] \sin(\phi_{\gamma} - \phi_S)}{\int d\phi_{\gamma} [D(x_F, M, q_T)]}$$

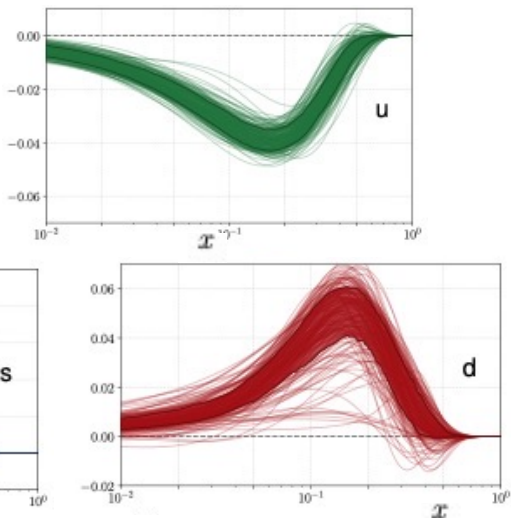
$$\begin{aligned} N(x_F, M, q_T, \phi_{\gamma}) &\equiv \frac{d^4\sigma^{\uparrow}}{dx_F dM^2 d^2\mathbf{q}_T} - \frac{d^4\sigma^{\downarrow}}{dx_F dM^2 d^2\mathbf{q}_T} \\ &= \frac{4\pi\alpha^2}{9M^2s} \sum_q \frac{e_q^2}{x_1 + x_2} \Delta^N f_{q/A^{\uparrow}}(x_1) f_{\bar{q}/B}(x_2) \sqrt{2e} \frac{q_T}{M_1} \frac{\langle k_S^2 \rangle^2 \exp[-q_T^2 / (\langle k_S^2 \rangle + \langle k_{\perp 2}^2 \rangle)]}{\pi [\langle k_S^2 \rangle + \langle k_{\perp 2}^2 \rangle]^2 \langle k_{\perp 2}^2 \rangle} \sin(\phi_S - \phi_{\gamma}) \end{aligned}$$

$$\begin{aligned} D(x_F, M, q_T) &\equiv \frac{1}{2} \left[ \frac{d^4\sigma^{\uparrow}}{dx_F dM^2 d^2\mathbf{q}_T} + \frac{d^4\sigma^{\downarrow}}{dx_F dM^2 d^2\mathbf{q}_T} \right] = \frac{d^4\sigma^{unp}}{dx_F dM^2 d^2\mathbf{q}_T} \\ &= \frac{4\pi\alpha^2}{9M^2s} \sum_q \frac{e_q^2}{x_1 + x_2} f_{q/A}(x_1) f_{\bar{q}/B}(x_2) \frac{\exp[-q_T^2 / (\langle k_{\perp 1}^2 \rangle + \langle k_{\perp 2}^2 \rangle)]}{\pi [\langle k_{\perp 1}^2 \rangle + \langle k_{\perp 2}^2 \rangle]} \end{aligned}$$



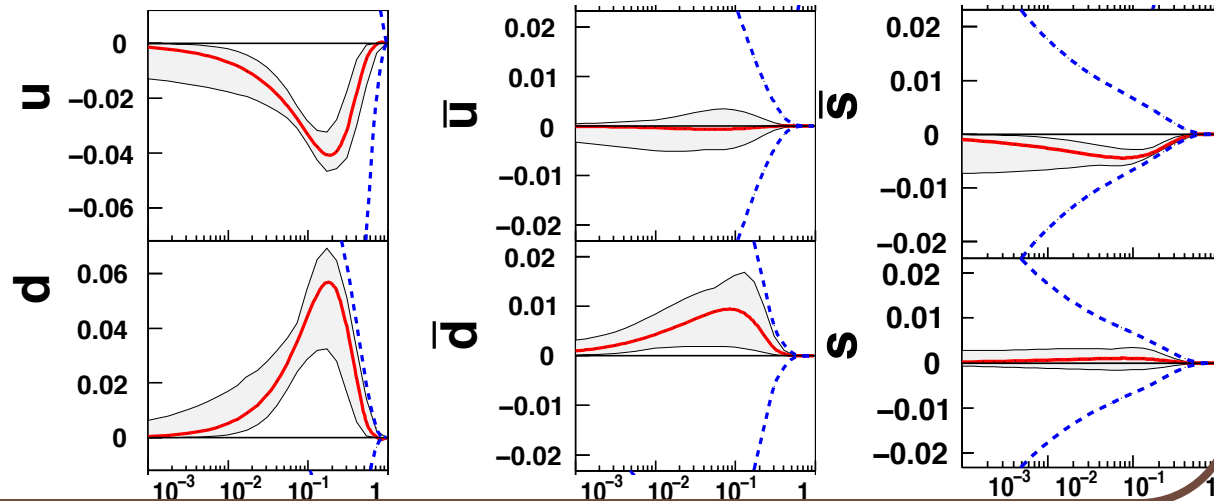
# GLOBAL ANALYSES OF SIVERS FUNCTION

A. Bacchetta, F. Delcarro, C. Pasiano, M. Radici  
arXiv 2004.14278 (2020)

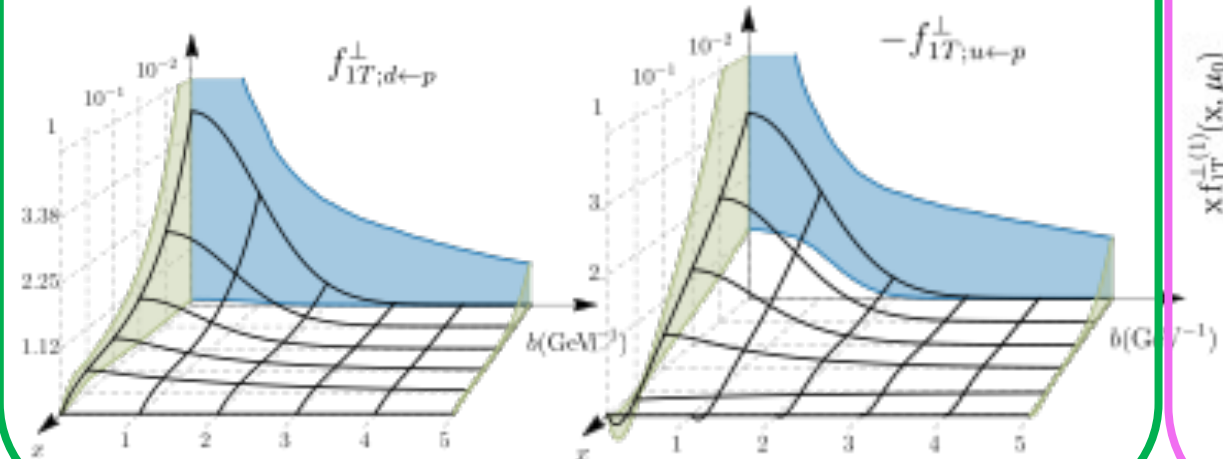


HERMES (2020)  
COMPASS (2009)  
COMPASS (2015)  
JLab (2011)

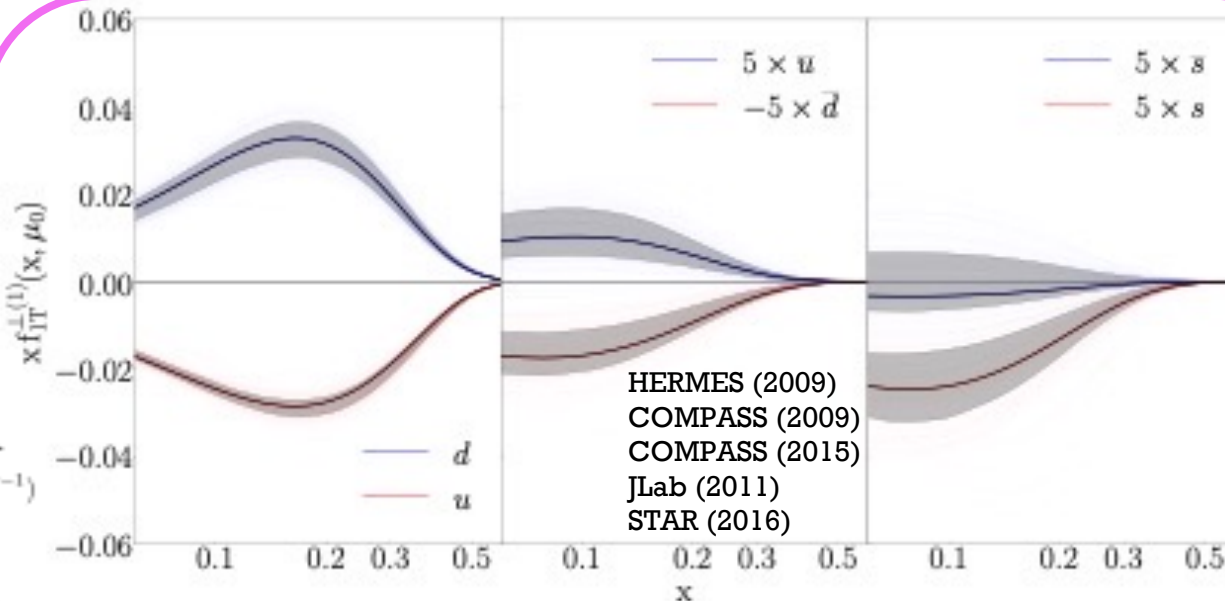
M. Anselmino, M. Boglion, U. D'Alesio, S. Melis, F. Murgia, A. Prokudin\_PRD\_79\_54010\_(2009)



HERMES (2020), COMPASS (2009), COMPASS (2015)  
JLab (2011), STAR (2016), COMPASS DY (2017)



M. Bury, A. Prokudin, A. Vladimirov, JHEP\_05\_151 (2021)



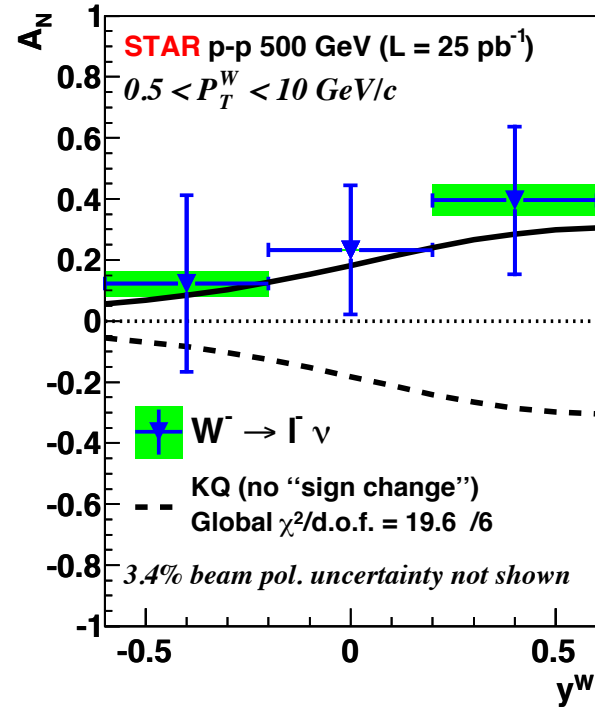
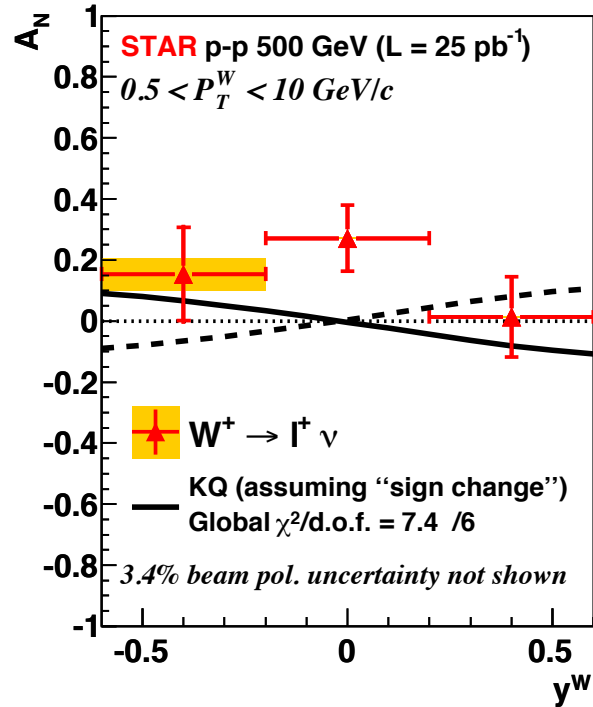
HERMES (2009)  
COMPASS (2009)  
COMPASS (2015)  
JLab (2011)  
STAR (2016)

M. Echevarria, Z. Kang, J. Terry\_JHEP\_01\_126\_(2021)

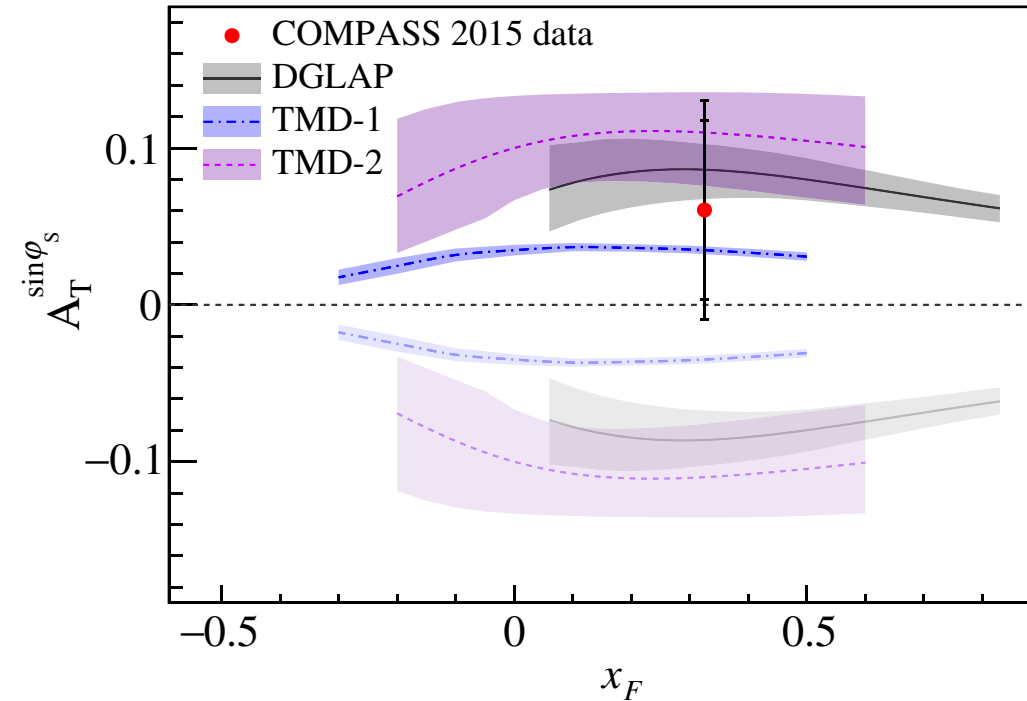


# SIGN OF SIVERS FUNCTIONS

STAR Collaboration (PRL 116 132301 (2016))



COMPASS Collaboration (PRL 119 112002 (2017))



TSSA amplitude for  $W^+/W^-$  from STAR data is favors the “sign-change”  
 In DY relative to SIDIS (model based without TMD evolution)

Dark Shaded (Light-shaded):  
 with(without)  
 “sign-change”



# FITTING METHODOLOGY

## Inputs:

- Unpolarized PDFs : LHAPDF6 (CTEQ61)
- Fragmentation Functions:
  - Pi+: NNFF10\_Pip\_nlo
  - Pi- : NNFF10\_Pim\_nlo
  - Pi0: NNFF10\_Pisum\_nlo
  - K+: NNFF10\_Kap\_nlo
  - K- : NNFF10\_Kam\_nlo

*V. Bertone et. al arXiv:1706.07049*

## Data Sets (on consideration):

### SIDIS

- HERMES\_p\_2009 (from Luciano Pappalardo)
- COMPASS\_d\_2009 (from Bakur Parsamyan )
- COMPASS\_p\_2015 (from Bakur Parsamyan )
- HERMES\_p\_2020 (from Luciano Pappalardo)

### DY

- COMPASS\_2017 (from Bakur Parsamyan )

## Fit parameters (13):

$$M_1$$

$$N_u, \alpha_u, \beta_u, N_{\bar{u}}$$

$$N_d, \alpha_d, \beta_d, N_{\bar{d}}$$

$$N_s, \alpha_s, \beta_s, N_{\bar{s}}$$

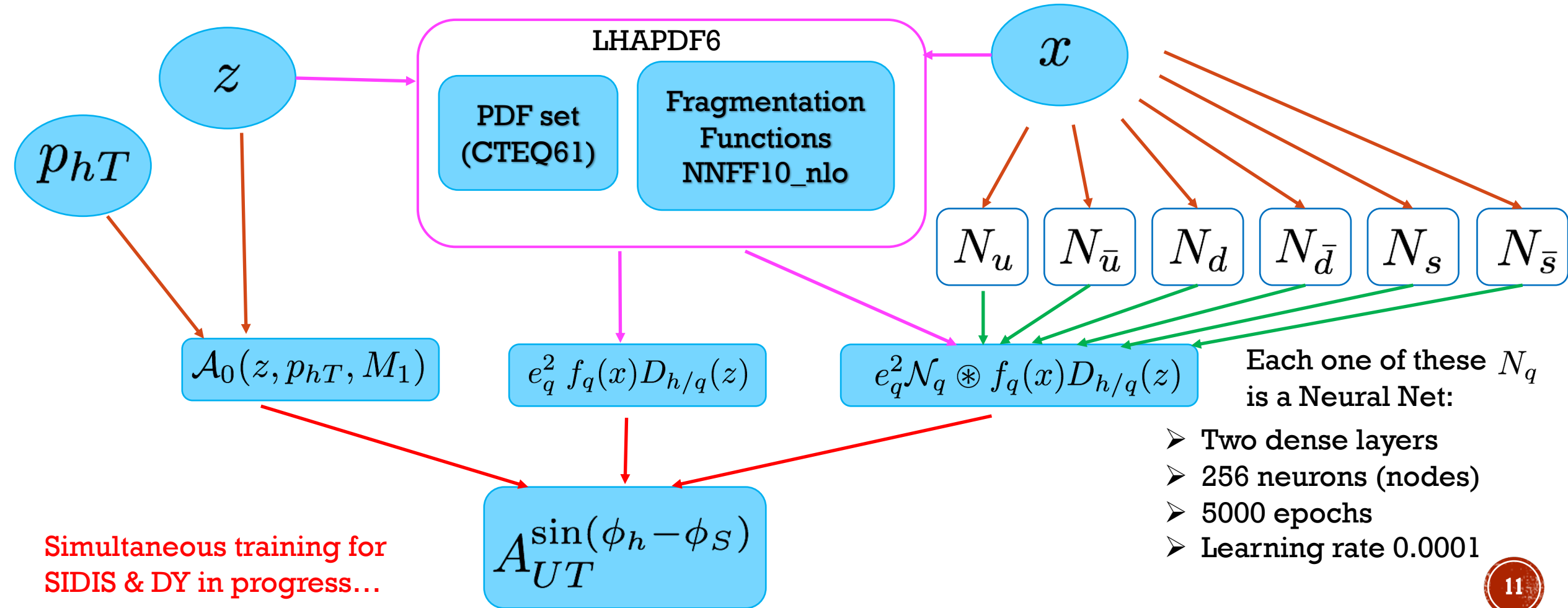
## Fitting routines:

- “iminuit” (python supported version of MINUIT)  
Treated the  $N_q$  in the same way as Anselmino et al’s approach
- Using a Neural Network approach  
 $\mathcal{N}_{\bar{q}}(x)$  and  $\mathcal{N}_{\bar{q}}(x)$  were treated as analogous & separate NN models for quarks and anti-quarks  
(‘x’ as an input)

# NEURAL NETWORK APPROACH WITH SIDIS DATA

Motivation for ANN

$$A_{UT}^{\sin(\phi_h - \phi_S)}(x, y, z, p_{hT}) = \mathcal{A}_0(z, p_{hT}, M_1) \left( \frac{\sum_q \mathcal{N}_q e_q^2 f_q(x) D_{h/q}(z)}{\sum_q e_q^2 f_q(x) D_{h/q}(z)} \right)$$



Simultaneous training for SIDIS & DY in progress...

# FITS TO SIDIS DATA : INITIAL ATTEMPTS

## Individual fits

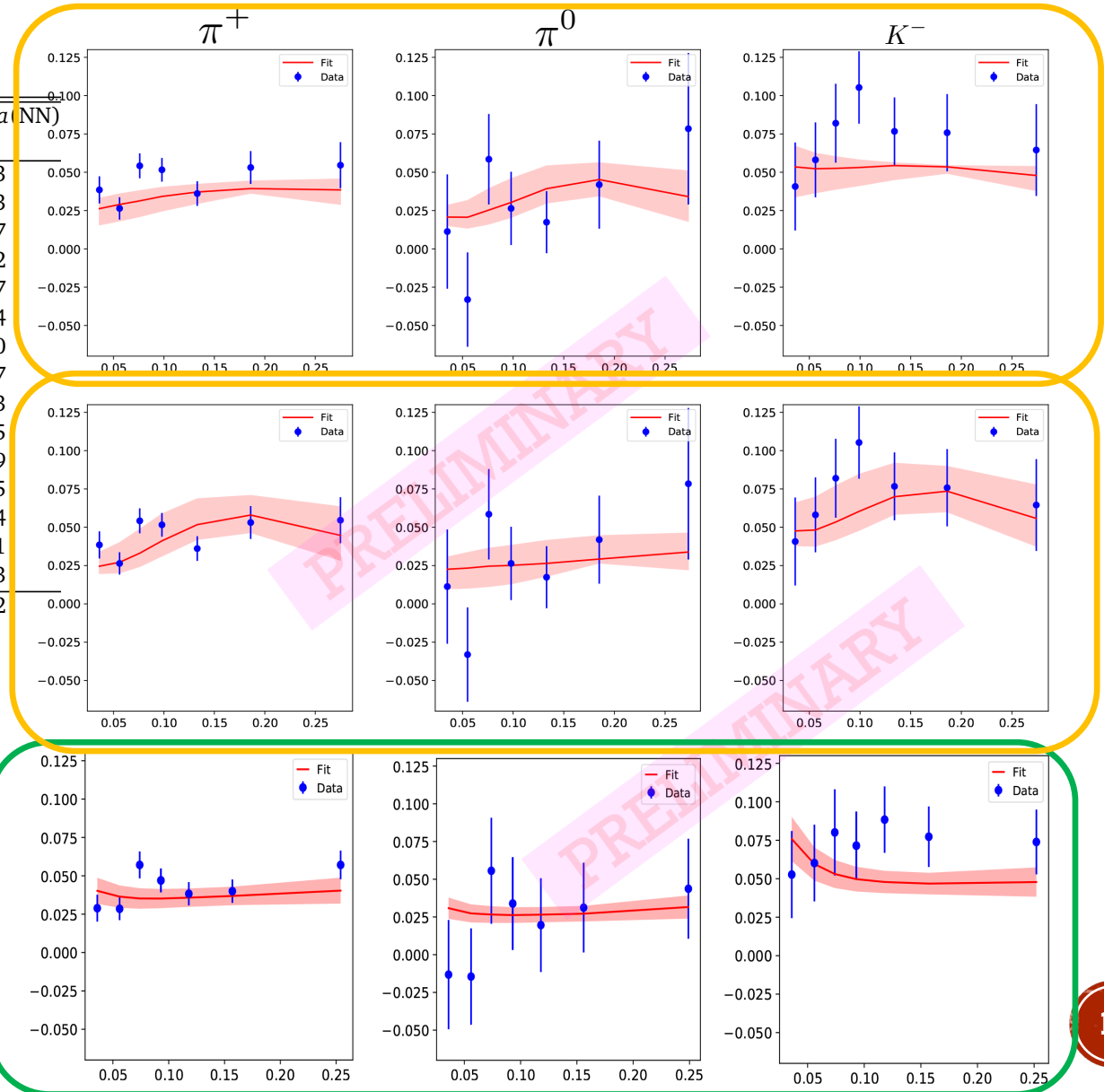
HERMES 2009

HERMES 2020

Hadron	Dependence	HERMES2009		HERMES2020	
		ndata	$\chi^2/ndata$	$\chi^2/ndata$	$\chi^2/ndata$
$\pi^+$	$x$	7	2.53	8	2.12
$\pi^+$	$z$	7	1.02	11	1.49
$\pi^+$	$P_{hT}$	7	5.23	8	1.14
$\pi^-$	$x$	7	1.94	8	1.81
$\pi^-$	$z$	7	2.45	11	1.16
$\pi^-$	$P_{hT}$	7	1.61	8	1.20
$\pi^0$	$x$	7	0.85	8	0.40
$\pi^0$	$z$	7	1.11	11	0.95
$\pi^0$	$P_{hT}$	7	2.00	8	0.50
$K^+$	$x$	7	1.22	8	0.48
$K^+$	$z$	7	2.97	11	6.31
$K^+$	$P_{hT}$	7	2.65	8	1.26
$K^-$	$x$	7	0.49	8	0.26
$K^-$	$z$	7	0.52	10	0.93
$K^-$	$P_{hT}$	7	0.96	8	0.79
Total		105	1.84	134	1.477

Parameter	HERMES 2009	HERMES2020
$M_1$	$1.303 \pm 0.010$	$7.590 \pm 0.008$
$N_u$	$0.169 \pm 0.002$	$0.960 \pm 0.084$
$\alpha_u$	$0.645 \pm 0.125$	$2.291 \pm 0.200$
$\beta_u$	$3.122 \pm 2.661$	$9.826 \pm 1.556$
$N_{\bar{u}}$	$0.007 \pm 0.003$	$0.205 \pm 0.02$
$N_d$	$-0.434 \pm 0.005$	$-4.713 \pm 0.004$
$\alpha_d$	$1.777 \pm 0.909$	$0.482 \pm 0.866$
$\beta_d$	$7.788 \pm 2.144$	$(5.675 \pm 6.45) \times 10^{-6}$
$N_{\bar{d}}$	$-0.142 \pm 0.048$	$1.490 \pm 0.05$
$N_s$	$0.563 \pm 0.073$	$4.528 \pm 0.073$
$\alpha_s$	$(6.84 \pm 10.00) \times 10^{-5}$	$(1.745 \pm 9.20) \times 10^{-5}$
$\beta_s$	$(5.987 \pm 8.77) \times 10^{-10}$	$(6.082 \pm 9.55) \times 10^{-10}$
$N_{\bar{s}}$	$-0.122 \pm 0.504$	$8.692 \pm 0.46$

Projected Asymmetries For HERMES 2020 Trained based on HERMES 2009

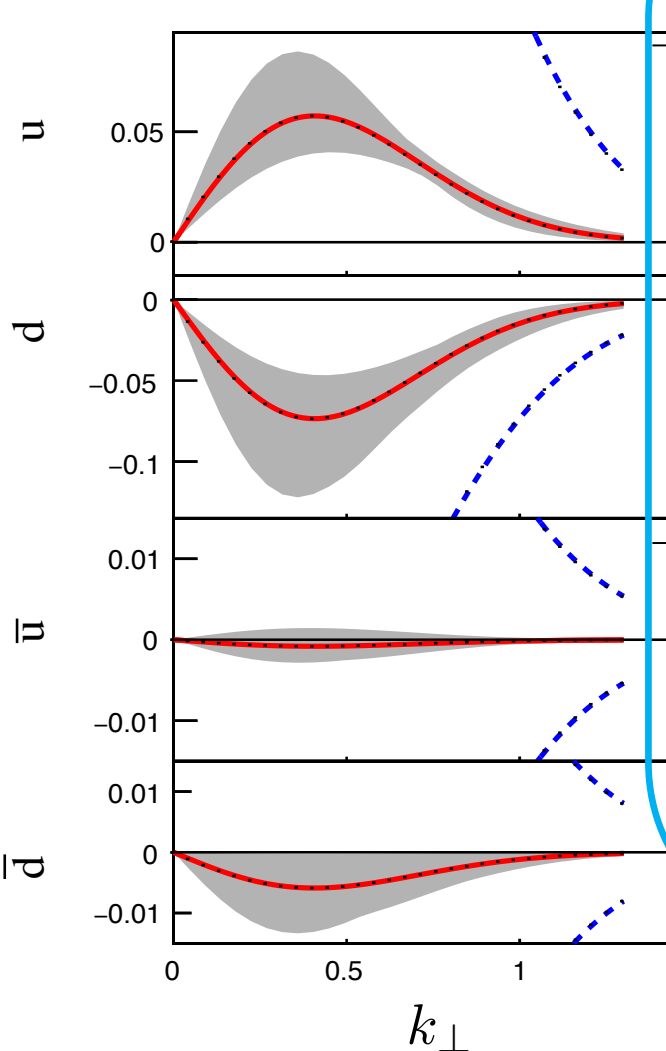


# GLOBAL FIT TO SIDIS DATA

HERMES2009, COMPASS2009,  
COMPASS2015

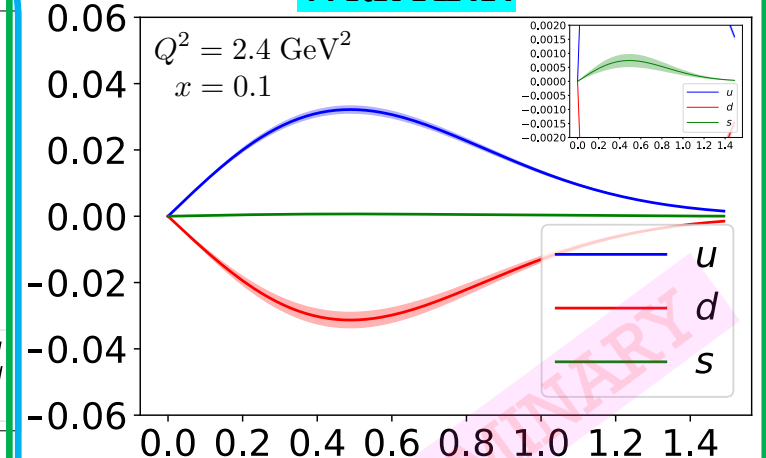
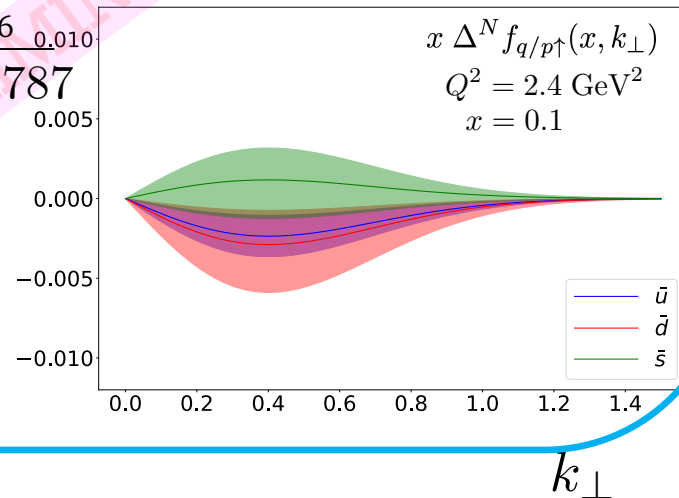
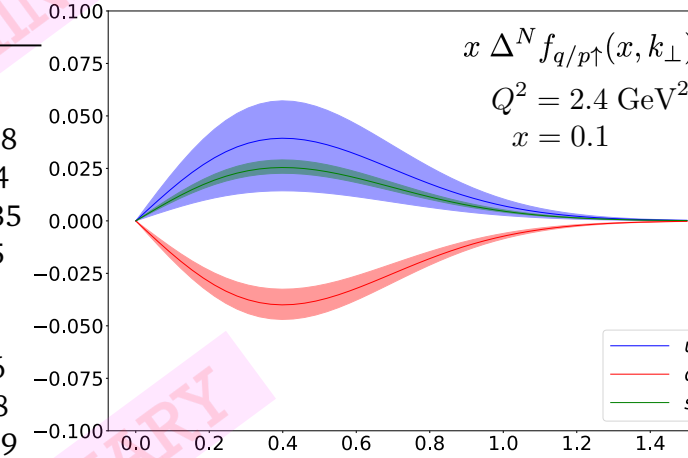
HERMES2009, **HERMES2020**  
COMPASS2009, COMPASS2015

HERMES2009, **HERMES2020**  
COMPASS2009, COMPASS2015  
**With ANN**

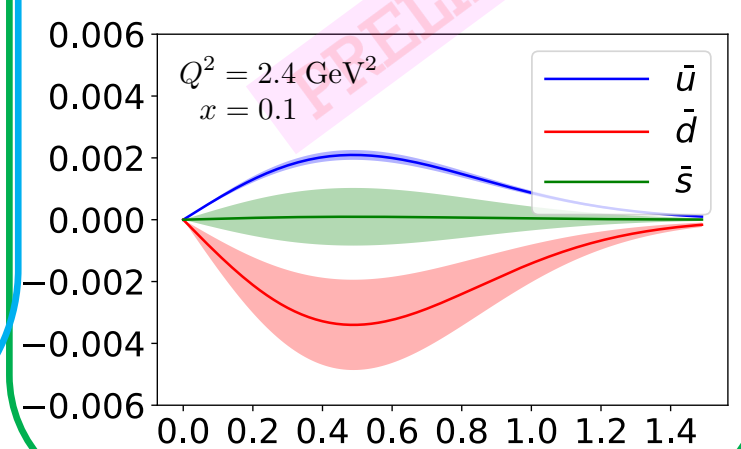


Parameter	Value
$M_1$	$5.35 \pm 0.16$
$N_u$	$0.62 \pm 0.12$
$\alpha_u$	$2.537 \pm 0.018$
$\beta_u$	$13.82 \pm 0.14$
$N_{\bar{u}}$	$-0.189 \pm 0.035$
$N_d$	$-1.15 \pm 0.05$
$\alpha_d$	$2.2 \pm 0.05$
$\beta_d$	$9.12 \pm 0.33$
$N_{\bar{d}}$	$-0.16 \pm 0.06$
$N_s$	$10.09 \pm 0.18$
$\alpha_s$	$0.497 \pm 0.019$
$\beta_s$	$0.066 \pm 0.004$
$N_{\bar{s}}$	$0.18 \pm 0.16$

$\chi^2/\text{NDF} = 1.787$



NN Trained 90% of SIDIS Loss  $\sim 1.9$



ANN: with 100 replicas  $\rightarrow$  need to generate with higher number of replicas

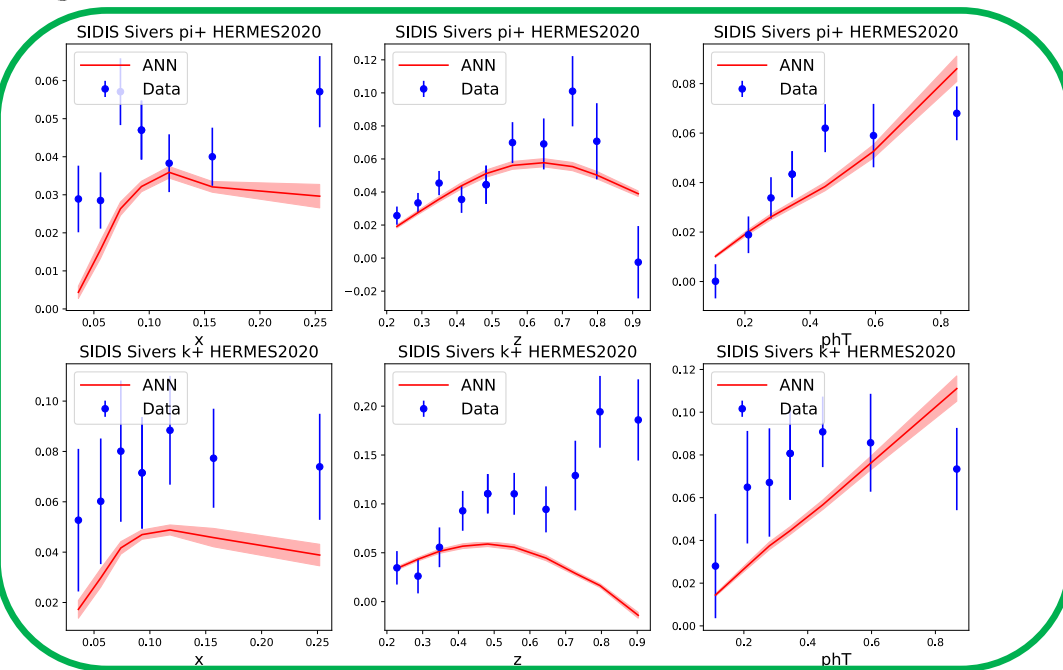
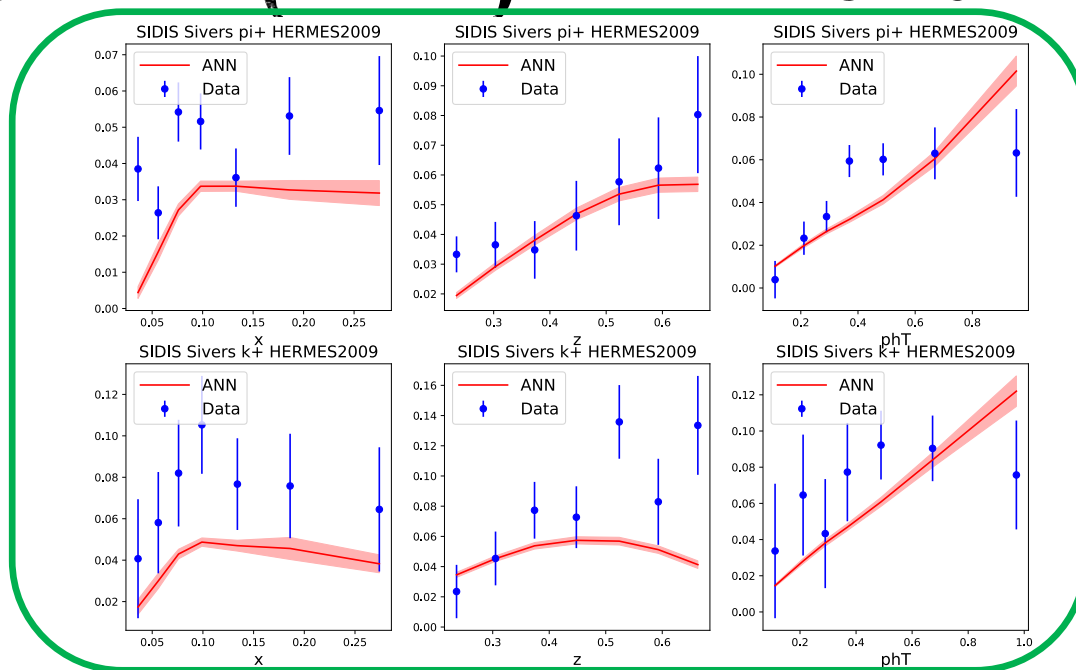
**PRELIMINARY**

# GLOBAL (ANN) FIT TO SIDIS DATA

PRELIMINARY

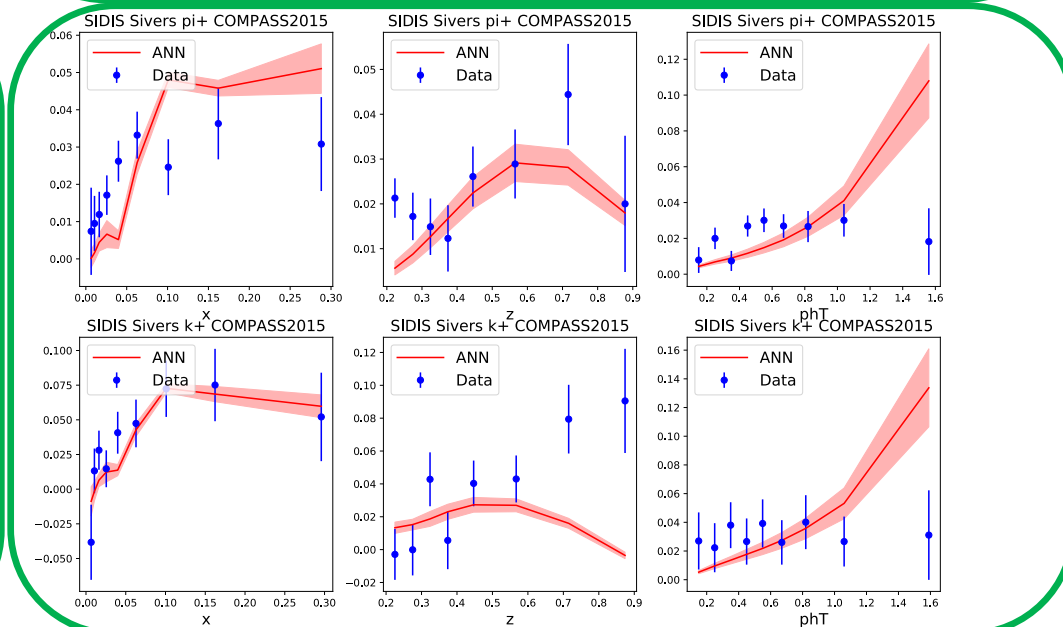
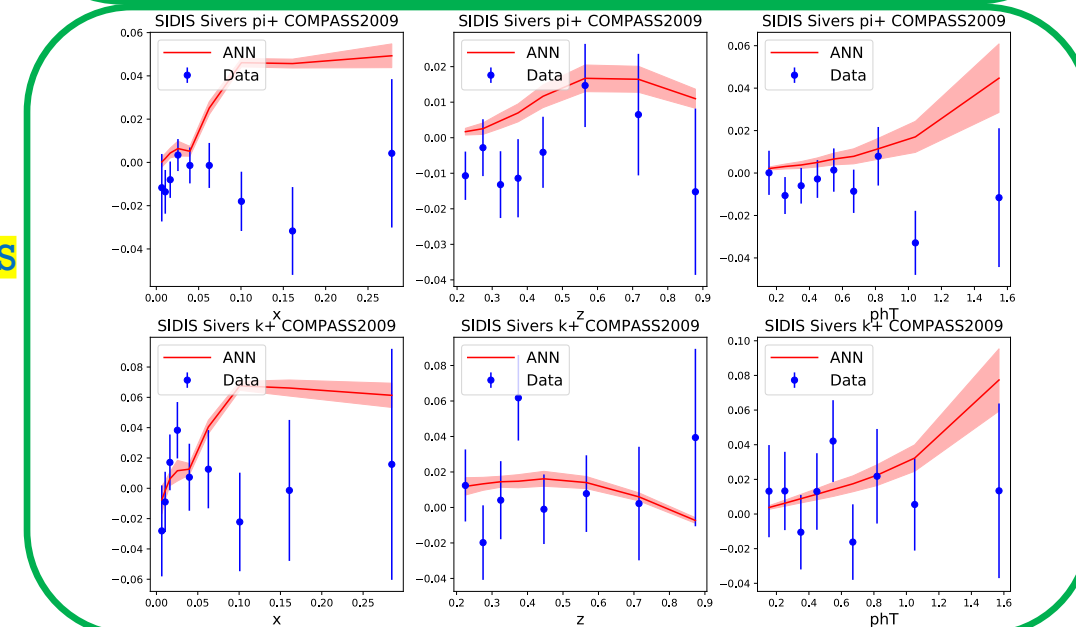
HERMES  
2009

HERMES  
2020



COMPASS  
2009

COMPASS  
2015

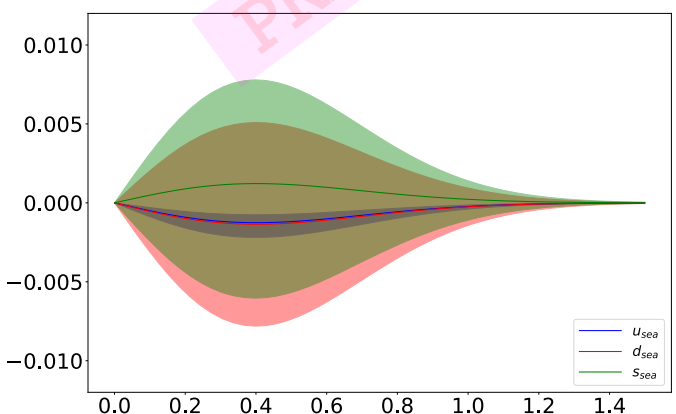
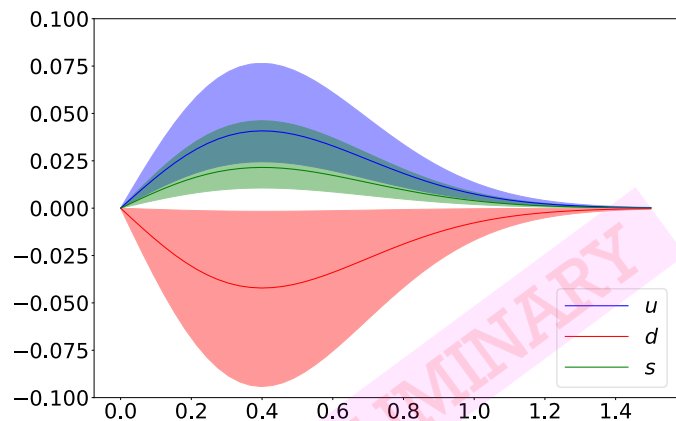




# GLOBAL FIT TO SIDIS & DY DATA

PRELIMINARY

With sign change

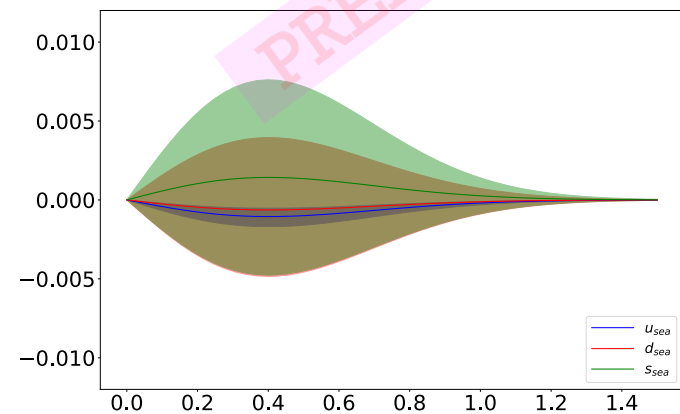
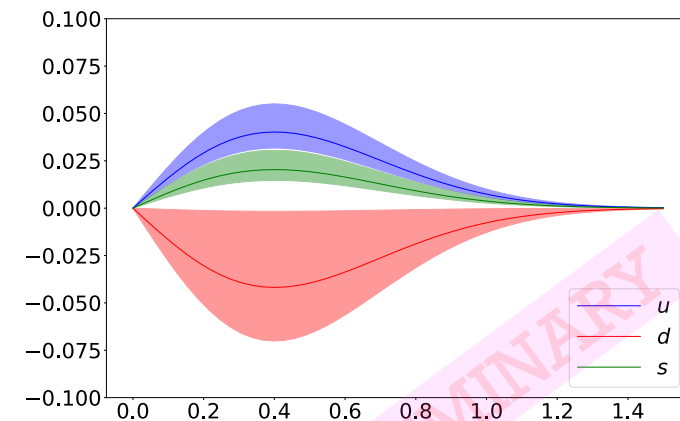


Parameter	sign-flip	no-sign-flip
$M_1$	$5.7 \pm 0.8$	$6.1 \pm 0.5$
$N_u$	$0.69 \pm 0.08$	$0.72 \pm 0.05$
$\alpha_u$	$2.74 \pm 0.09$	$2.71 \pm 0.05$
$\beta_u$	$15.1 \pm 0.6$	$15.05 \pm 0.30$
$N_{\bar{u}}$	$-0.107 \pm 0.017$	$-0.096 \pm 0.018$
$N_d$	$-1.34 \pm 0.15$	$-1.30 \pm 0.11$
$\alpha_d$	$1.6 \pm 0.4$	$1.36 \pm 0.31$
$\beta_d$	$5.4 \pm 2.5$	$4.7 \pm 1.8$
$N_{\bar{d}}$	$-0.08 \pm 0.13$	$-0.04 \pm 0.12$
$N_s$	$11.2 \pm 1.4$	$12.0 \pm 0.9$
$\alpha_s$	$0.85 \pm 0.09$	$0.91 \pm 0.05$
$\beta_s$	$0.46 \pm 0.12$	$0.52 \pm 0.07$
$N_{\bar{s}}$	$0.2 \pm 0.4$	$0.25 \pm 0.32$
$\chi^2/N$	1.871	1.870

Ongoing work:

- Analyzing the fit results & optimizing the fitting framework
- DY extension to the SIDIS NN model

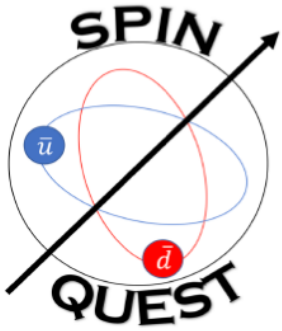
Without sign change



$k_{\perp}$

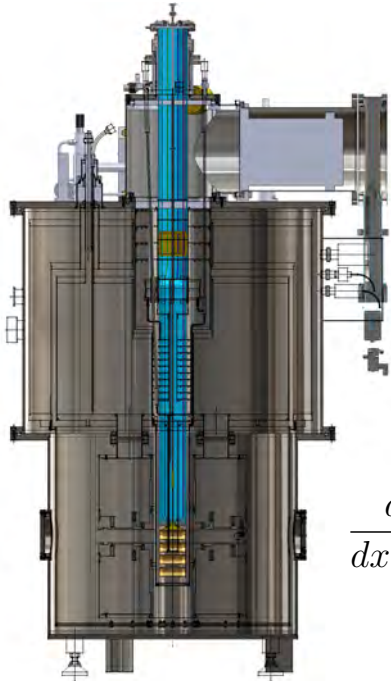
# DISCUSSION & FUTURE WORK

- Simultaneous fits to SIDIS and DY data with higher statistics of replicas
- Improving the Neural Network to train simultaneously on both SIDIS & DY data with optimizing hyperparameters with higher statistics of replicas.
- Investigating towards Sivers Asymmetry extraction from Drell –Yan with/without considering the “sign-flip” of the Sivers Function.
- Simultaneous fits to Sivers function and Boer-Mulders function.



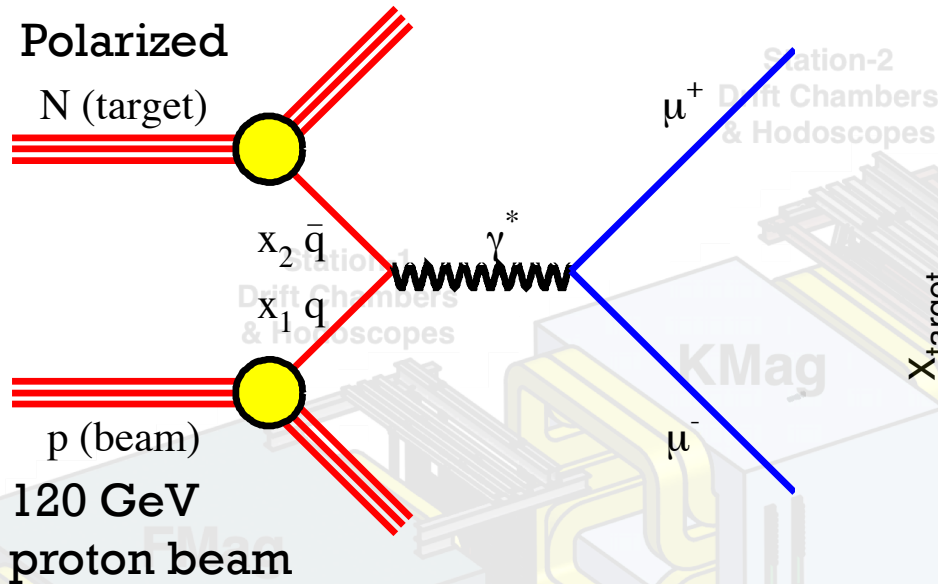
# SPINQUEST (E1039) EXPERIMENT AT FERMILAB

➤ Measurement of 'sea' quark Sivers function



LANL-UVA  
Polarized Target

$$pp \uparrow (d^\uparrow) \rightarrow \mu^+ \mu^- X, 4 < M_{\mu\mu} < 9 \text{ GeV}$$



$$\frac{d\sigma}{dx_1 dx_2} = \frac{4\pi\alpha^2}{9sx_1x_2} \sum_i e_i^2 (q_i^B(x_1, Q^2) \bar{q}_i^T(x_2, Q^2) + \bar{q}_i^B(x_1, Q^2) q_i^T(x_2, Q^2))$$

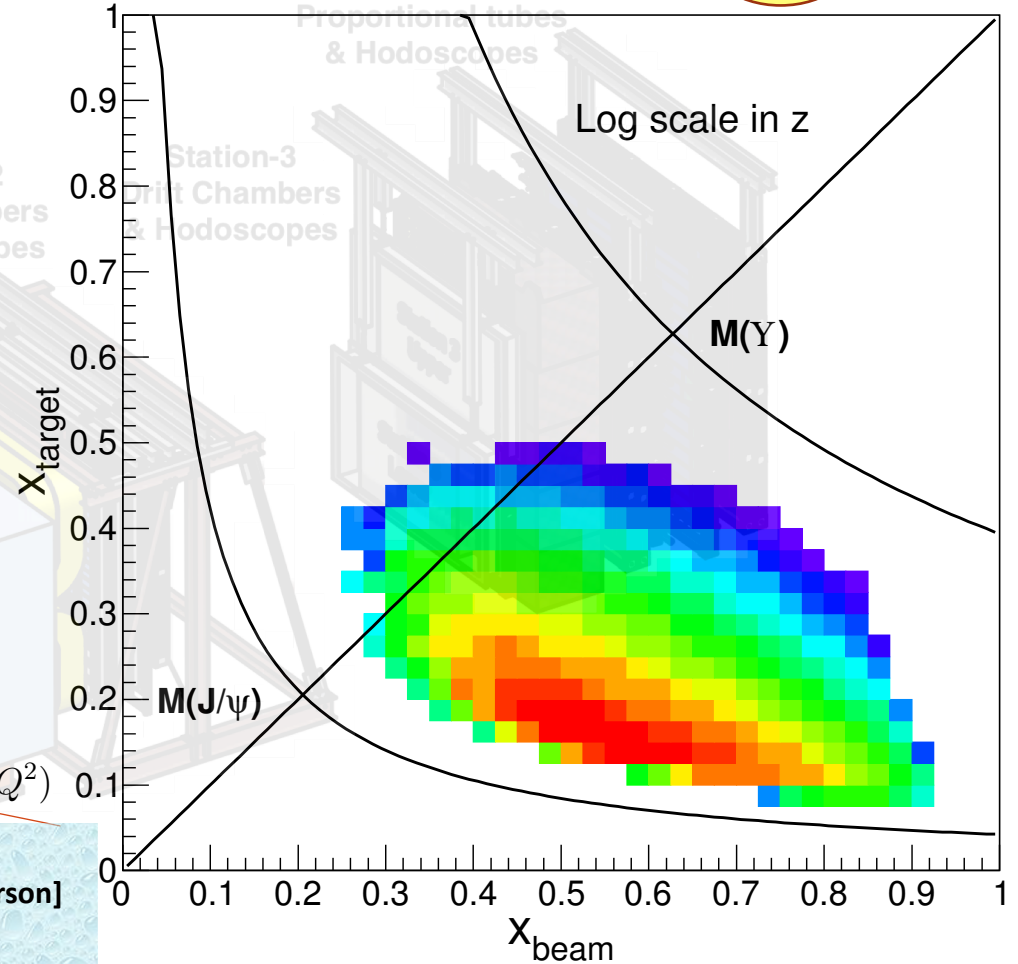
Please Join The Effort

Dustin Keller ([dustin@virginia.edu](mailto:dustin@virginia.edu))[Spokesperson]

Kun Liu ([Spokesperson])

<https://spinquest.fnal.gov/>

<http://twist.phys.virginia.edu/E1039/>



*Thank you*



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**ENERGY**

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Science

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